

Insiemi noti (calcolabilità)

- $K = \{x \mid \varphi_x(x) \downarrow\}$, \mathcal{RE} -completo, $K \not\leq \overline{K}$, $\overline{K} \notin \mathcal{RE}$
- $\overline{K} \in \text{co-}\mathcal{RE}$
- $K_0 = \{(x, y) \mid \varphi_x(y) \downarrow\}$
- $K_1 = \{x \mid \text{dom}(\varphi_x) \neq \emptyset\}$, $K_1 \in \underset{\text{colomba}}{\mathcal{RE}} \setminus \underset{\text{Rice}}{\mathcal{R}}$
- $K \equiv K_0 \equiv K_1$, quindi tutti \mathcal{RE} -completi
- $\text{TOT} = \{x \mid \varphi_x \in \text{rec}\}$, $K \leq \text{TOT}$, $\text{TOT} \notin \mathcal{RE}$ perché $K \leq \text{TOT}$ e $K \leq \overline{\text{TOT}}$, quindi anche $\overline{K} \leq \text{TOT}$, allora se $\text{TOT} \in \mathcal{RE}$, $K, \overline{K} \in \mathcal{RE}$ e $K \in \mathcal{R}$ — assurdo
- $\text{FIN} = \{x \mid \text{dom}(\varphi_x) \text{ finito}\}$
- $\text{INF} = \{x \mid \text{dom}(\varphi_x) \text{ infinito}\}$
- $\text{REC} = \{x \mid \text{dom}(\varphi_x) \in \mathcal{R}\}$
- $\text{COST} = \{x \mid \exists y . \forall z . \varphi_x(z) = y\}$
- $\text{EXT} = \{x \mid \varphi_x \text{ estendibile a funzione calcolabile totale}\}$
- $\overline{K} \leq \text{TOT}, \text{FIN}, \text{INF}, \text{REC}, \text{COST}, \text{EXT}$, quindi non sono \mathcal{RE}